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PAL — Positional Astronomy Library

0.1.0

Programmer's Manual

Abstract

PAL provides a subset of the Fortran SLALIB library but written in C using the SLALIB C API. Where possible the PAL routines are implemented using the C SOFA library. It is provided with a GPL license.

1 Introduction

This library provides a C library designed as a API-compatible replacement for the C SLALIB library (SUN/67) and uses a GPL licence so is freely redistributable. Where possible the functions call equivalent SOFA routines (Hohenkerk, C., 2011, Scholarpedia, **6**, 11404) and use current IAU 2006 standards. This means that any functions that rely on nutation or precession will return slightly different answers to the SLA functions.

2 Citing PAL

If you use PAL in your work please consider citing it. The description paper for PAL is: *PAL: A Positional Astronomy Library*, Jenness, T. & Berry, D. S., in *Astronomical Data Analysis Software and Systems XXII*, Friedel, D. N. (ed), ASP Conf. Ser. **475**, p307.

A Function Descriptions

A.1 SOFA Mappings

The following table lists PAL/SLA functions that have direct replacements in SOFA. Whilst these routines are implemented in the PAL library using SOFA new code should probably call SOFA directly.

SLA/PAL	SOFA
palCldj	iauCal2jd
palDbear	iauPas
palDaf2r	iauAf2a
palDav2m	iauRv2m
palDcc2s	iauC2s
palDcs2c	iauS2c
palDd2tf	iauD2tf
palDimxv	iauTrxp
palDm2av	iauRm2v
palDjcl	iauJd2cal
palDmxm	iauRxr
palDmxv	iauRxp
palDpav	iauPap
palDr2af	iauA2af
palDr2tf	iauA2tf
palDranrm	iauAnp
palDsep	iauSeps
palDsepv	iauSepp
palDtf2d	iauTf2d
palDtf2r	iauTf2a
palDvdv	iauPdp
palDvn	iauPn
palDvxv	iauPxp
palEpb	iauEpb
palEpb2d	iauEpb2d
palEpj	iauEpj
palEpj2d	iauEpj2jd
palEeqqx	iauEe06a
palFk5hz	iauFk5hz <i>also calls iauEpj2jd</i>
palGmst	iauGmst06
palGmsta	iauGmst06
palHfk5z	iauHfk5z <i>also calls iauEpj2jd</i>

A.2 More complex functions

These functions do not have a simple equivalent in SOFA so are reimplemented either completely standalone or using multiple SOFA functions.

palAddet	Add the E-terms to a pre IAU 1976 mean place	palAddet
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Description: Add the E-terms (elliptic component of annual aberration) to a pre IAU 1976 mean place to conform to the old catalogue convention.

Invocation: `void palAddet (double rm, double dm, double eq, double *rc, double *dc);`

Arguments:

rm = double (Given)
RA without E-terms (radians)

dm = double (Given)
Dec without E-terms (radians)

eq = double (Given)
Besselian epoch of mean equator and equinox

rc = double * (Returned)
RA with E-terms included (radians)

dc = double * (Returned)
Dec with E-terms included (radians)

Notes:

Most star positions from pre-1984 optical catalogues (or derived from astrometry using such stars) embody the E-terms. If it is necessary to convert a formal mean place (for example a pulsar timing position) to one consistent with such a star catalogue, then the RA,Dec should be adjusted using this routine.

See Also:

Explanatory Supplement to the Astronomical Ephemeris, section 2D, page 48.

palAirmas	Air mass at given zenith distance	palAirmas
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Description: Calculates the airmass at the observed zenith distance.

Invocation: `double palAirmas(double zd);`

Arguments:

zd = double (Given)
Observed zenith distance (radians)

- The "observed" zenith distance referred to above means "as affected by refraction".
- Uses Hardie's (1962) polynomial fit to Bemporad's data for the relative air mass, X , in units of thickness at the zenith as tabulated by Schoenberg (1929). This is adequate for all normal needs as it is accurate to better than 0.1% up to $X = 6.8$ and better than 1% up to $X = 10$. Bemporad's tabulated values are unlikely to be trustworthy to such accuracy because of variations in density, pressure and other conditions in the atmosphere from those assumed in his work.
- The sign of the ZD is ignored.
- At zenith distances greater than about $ZD = 87$ degrees the air mass is held constant to avoid arithmetic overflows.

- Hardie, R.H., 1962, in "Astronomical Techniques" ed. W.A. Hiltner, University of Chicago Press, p180.
- Schoenberg, E., 1929, Hdb. d. Ap., Berlin, Julius Springer, 2, 268.

```

ra = double (Given)
    Apparent RA (radians)

dec = double (Given)
    Apparent Dec (radians)

date = double (Given)
    TDB for apparent place (JD-2400000.5)

eq = double (Given)
    Equinox: Julian epoch of mean place.

rm = double * (Returned)
    Mean RA (radians)

dm = double * (Returned)
    Mean Dec (radians)

```

Notes:

- See *palMappa* and *palAmpqk* for details.

palAmpqk	Convert star RA,Dec from geocentric apparent to mean place	palAmpqk
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Description: Convert star RA,Dec from geocentric apparent to mean place. The "mean" coordinate system is in fact close to ICRS. Use of this function is appropriate when efficiency is important and where many star positions are all to be transformed for one epoch and equinox. The star-independent parameters can be obtained by calling the *palMappa* function.

Invocation: `void palAmpqk (double ra, double da, double amprms[21], double *rm,
double *dm)`

Arguments:

ra = double (Given)

Apparent RA (radians).

da = double (Given)

Apparent Dec (radians).

amprms = double[21] (Given)

Star-independent mean-to-apparent parameters (see *palMappa*): (0) time interval for proper motion (Julian years) (1-3) barycentric position of the Earth (AU) (4-6) not used (7) not used (8-10) abv: barycentric Earth velocity in units of c (11) sqrt(1-v*v) where v=modulus(abv) (12-20) precession/nutation (3,3) matrix

rm = double (Returned)

Mean RA (radians).

dm = double (Returned)

Mean Dec (radians).

palCaldj	Gregorian Calendar to Modified Julian Date	palCaldj
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Description: Modified Julian Date to Gregorian Calendar with special behaviour for 2-digit years relating to 1950 to 2049.

Invocation: `void palCaldj (int iy, int im, int id, double *djm, int *j);`

Arguments:

iy = int (Given)

Year in the Gregorian calendar

im = int (Given)

Month in the Gergorian calendar

id = int (Given)
 Day in the Gregorian calendar

djm = double * (Returned)
 Modified Julian Date (JD-2400000.5) for 0 hrs

j = status (Returned)
 0 = OK. See iauCal2jd for other values.

Notes:

- Uses iauCal2jd
- Unlike iauCal2jd this routine treats the years 0-100 as referring to the end of the 20th Century and beginning of the 21st Century. If this behaviour is not acceptable use the SOFA routine directly or palCldj. Acceptable years are 00-49, interpreted as 2000-2049, 50-99, " " 1950-1999, all others, interpreted literally.
- Unlike SLA this routine will work with negative years.

palDafin Sexagesimal character string to angle **palDafin**

Description: Extracts an angle from a sexagesimal string with degrees, arcmin, arcsec fields using space or comma delimiters.

Invocation: `void palDafin (const char *string, int *ipos, double *a, int *j);`

Arguments:

string = const char * (Given)
 String containing deg, arcmin, arcsec fields

ipos = int * (Given & Returned)
 Position to start decoding "string". First character is position 1 for compatibility with SLA. After calling this routine "iptr" will be positioned after the sexagesimal string.

a = double * (Returned)
 Angle in radians.

j = int * (Returned)
 status: 0 = OK +1 = default, A unchanged

- 1 = bad degrees)
- 2 = bad arcminutes) (note 3)
- 3 = bad arcseconds)

Notes:

- The first three "fields" in STRING are degrees, arcminutes, arcseconds, separated by spaces or commas. The degrees field may be signed, but not the others. The decoding is carried out by the palDftin routine and is free-format.

- Successive fields may be absent, defaulting to zero. For zero status, the only combinations allowed are degrees alone, degrees and arcminutes, and all three fields present. If all three fields are omitted, a status of +1 is returned and A is unchanged. In all other cases A is changed.
- Range checking:

The degrees field is not range checked. However, it is expected to be integral unless the other two fields are absent.

The arcminutes field is expected to be 0-59, and integral if the arcseconds field is present. If the arcseconds field is absent, the arcminutes is expected to be 0-59.9999...

The arcseconds field is expected to be 0-59.9999...

- Decoding continues even when a check has failed. Under these circumstances the field takes the supplied value, defaulting to zero, and the result A is computed and returned.
- Further fields after the three expected ones are not treated as an error. The pointer IPOS is left in the correct state for further decoding with the present routine or with *palDflt* etc. See the example, above.
- If STRING contains hours, minutes, seconds instead of degrees etc, or if the required units are turns (or days) instead of radians, the result A should be multiplied as follows:

for to obtain multiply STRING A in A by

d ' " radians 1 = 1.0 d ' " turns 1/2pi = 0.1591549430918953358 h m s radians 15 = 15.0
h m s days 15/2pi = 2.3873241463784300365

Example:

argument before after

STRING '-57 17 44.806 12 34 56.7' unchanged IPTR 1 16 (points to 12...) A ? -1.00000D0
J ? 0

palDe2h	Equatorial to horizon coordinates: HA,Dec to Az,E	palDe2h
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Description: Convert equatorial to horizon coordinates.

Invocation: `palDe2h(double ha, double dec, double phi, double * az, double * el
);`

Arguments:

ha = double * (Given)
Hour angle (radians)

dec = double * (Given)
Declination (radians)

```

phi = double (Given)
    Observatory latitude (radians)
az = double * (Returned)
    Azimuth (radians)
el = double * (Returned)
    Elevation (radians)

```

Notes:

- All the arguments are angles in radians.
- Azimuth is returned in the range 0-2pi; north is zero, and east is +pi/2. Elevation is returned in the range +/-pi/2.
- The latitude must be geodetic. In critical applications, corrections for polar motion should be applied.
- In some applications it will be important to specify the correct type of hour angle and declination in order to produce the required type of azimuth and elevation. In particular, it may be important to distinguish between elevation as affected by refraction, which would require the "observed" HA,Dec, and the elevation in vacuo, which would require the "topocentric" HA,Dec. If the effects of diurnal aberration can be neglected, the "apparent" HA,Dec may be used instead of the topocentric HA,Dec.
- No range checking of arguments is carried out.
- In applications which involve many such calculations, rather than calling the present routine it will be more efficient to use inline code, having previously computed fixed terms such as sine and cosine of latitude, and (for tracking a star) sine and cosine of declination.

palDeuler Form a rotation matrix from the Euler angles **palDeuler**

Description: A rotation is positive when the reference frame rotates anticlockwise as seen looking towards the origin from the positive region of the specified axis.

The characters of ORDER define which axes the three successive rotations are about. A typical value is 'ZXZ', indicating that RMAT is to become the direction cosine matrix corresponding to rotations of the reference frame through PHI radians about the old Z-axis, followed by THETA radians about the resulting X-axis, then PSI radians about the resulting Z-axis.

The axis names can be any of the following, in any order or combination: X, Y, Z, uppercase or lowercase, 1, 2, 3. Normal axis labelling/numbering conventions apply; the xyz (=123) triad is right-handed. Thus, the 'ZXZ' example given above could be written 'zxz' or '313' (or even 'ZxZ' or '3xZ'). ORDER is terminated by length or by the first unrecognized character.

Fewer than three rotations are acceptable, in which case the later angle arguments are ignored. If all rotations are zero, the identity matrix is produced.

Invocation: `void palDeuler (const char *order, double phi, double theta, double psi, double rmat[3][3]);`

Arguments:

order = const char[] (Given)
 Specifies about which axes the rotation occurs

phi = double (Given)
 1st rotation (radians)

theta = double (Given)
 2nd rotation (radians)

psi = double (Given)
 3rd rotation (radians)

rmat = double[3][3] (Given & Returned)
 Rotation matrix

palDfltIn Convert free-format input into double precision **palDfltIn**
 floating point

Description: Extracts a number from an input string starting at the specified index.

Invocation: `void palDfltIn(const char * string, int *nstrt, double *dreslt, int *jflag);`

Arguments:

string = const char * (Given)
 String containing number to be decoded.

nstrt = int * (Given and Returned)
 Character number indicating where decoding should start. On output its value is updated to be the location of the possible next value. For compatibility with SLA the first character is index 1.

dreslt = double * (Returned)
 Result. Not updated when jflag=1.

jflag = int * (Returned)
 status: -1 = -OK, 0 = +OK, 1 = null, 2 = error

Notes:

- Uses the strtod() system call to do the parsing. This may lead to subtle differences when compared to the SLA/F parsing.
- All "D" characters are converted to "E" to handle fortran exponents.
- Commas are recognized as a special case and are skipped if one happens to be the next character when updating nstrt. Additionally the output nstrt position will skip past any trailing space.

- palDh2e Horizon to equatorial coordinates: Az,El to palDh2e
HA,Dec

Invocation: palDh2e(double az, double el, double phi, double * ha, double * dec
);

```

az = double (Given)
    Azimuth (radians)
el = double (Given)
    Elevation (radians)
phi = double (Given)
    Observatory latitude (radians)
ha = double * (Returned)
    Hour angle (radians)
dec = double * (Returned)
    Declination (radians)

```

- All the arguments are angles in radians.
- The sign convention for azimuth is north zero, east $+\pi/2$.
- HA is returned in the range $+\pi/-\pi$. Declination is returned in the range $+\pi/-\pi$.
- The latitude is (in principle) geodetic. In critical applications, corrections for polar motion should be applied.
- In some applications it will be important to specify the correct type of elevation in order to produce the required type of HA,Dec. In particular, it may be important to distinguish between the elevation as affected by refraction, which will yield the "observed" HA,Dec, and the elevation in vacuo, which will yield the "topocentric" HA,Dec. If the effects of diurnal aberration can be neglected, the topocentric HA,Dec may be used as an approximation to the "apparent" HA,Dec.
- No range checking of arguments is done.
- In applications which involve many such calculations, rather than calling the present routine it will be more efficient to use inline code, having previously computed fixed terms such as sine and cosine of latitude.

palDjcal Modified Julian Date to Gregorian Calendar **palDjcal**

Description: Modified Julian Date to Gregorian Calendar, expressed in a form convenient for formatting messages (namely rounded to a specified precision, and with the fields stored in a single array)

Invocation: `void palDjcal (int ndp, double djm, int iymdf[4], int *j);`

Arguments:

- ndp = int (Given)**
Number of decimal places of days in fraction.
- djm = double (Given)**
Modified Julian Date (JD-2400000.5)
- iymdf[4] = int[] (Returned)**
Year, month, day, fraction in Gregorian calendar.
- j = status (Returned)**
0 = OK. See iauJd2cal for other values.

Notes:

- Uses iauJd2cal

palDmat Matrix inversion & solution of simultaneous equations **palDmat**

Description: Matrix inversion & solution of simultaneous equations For the set of n simultaneous equations in n unknowns: $A \cdot Y = X$ this routine calculates the inverse of A, the determinant of matrix A and the vector of N unknowns.

Invocation: `void palDmat(int n, double *a, double *y, double *d, int *jf, int *iw);`

Arguments:

- n = int (Given)**
Number of simultaneous equations and number of unknowns.
- a = double[] (Given & Returned)**
A non-singular NxN matrix (implemented as a contiguous block of memory). After calling this routine "a" contains the inverse of the matrix.
- y = double[] (Given & Returned)**
The vector of N unknowns. On exit this vector contains the N solutions.
- d = double * (Returned)**
The determinant.
- jf = int * (Returned)**
The singularity flag. If the matrix is non-singular, jf=0 is returned. If the matrix is singular, jf=-1 & d=0.0 are returned. In the latter case, the contents of array "a" on return are undefined.

Notes:

- Implemented using Gaussian elimination with partial pivoting.
- Optimized for speed rather than accuracy with errors 1 to 4 times those of routines optimized for accuracy.

palDs2tp	Spherical to tangent plane projection	palDs2tp
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Description: Projection of spherical coordinates onto tangent plane: "gnomonic" projection - "standard coordinates"

Invocation: `palDs2tp(double ra, double dec, double raz, double decz, double *xi, double *eta, int *j);`

Arguments:

- ra = double (Given)**
RA spherical coordinate of point to be projected (radians)
- dec = double (Given)**
Dec spherical coordinate of point to be projected (radians)
- raz = double (Given)**
RA spherical coordinate of tangent point (radians)
- decz = double (Given)**
Dec spherical coordinate of tangent point (radians)
- xi = double * (Returned)**
First rectangular coordinate on tangent plane (radians)
- eta = double * (Returned)**
Second rectangular coordinate on tangent plane (radians)
- j = int * (Returned)**
status: 0 = OK, star on tangent plane 1 = error, star too far from axis 2 = error, antistar on tangent plane 3 = error, antistar too far from axis

palDtt	Return offset between UTC and TT	palDtt
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Description: Increment to be applied to Coordinated Universal Time UTC to give International Atomic Time (TAI).

Invocation: `dat = palDat(double utc);`

Arguments:

- utc = double (Given)**
UTC date as a modified JD (JD-2400000.5)

Returned Value:

- dat = double**
TAI-UTC in seconds

Notes:

- This routine converts the MJD argument to calendar date before calling the SOFA `iauDat` function.
- This routine matches the `slaDat` interface which differs from the `iauDat` interface. Consider coding directly to the SOFA interface.
- See `iauDat` for a description of error conditions when calling this function with a time outside of the UTC range.
- The status argument from `iauDat` is ignored. This is reasonable since the error codes are mainly related to incorrect calendar dates when calculating the JD internally.

palDmoon	Approximate geocentric position and velocity of the Moon	palDmoon
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Description: Calculate the approximate geocentric position of the Moon using a full implementation of the algorithm published by Meeus (1'Astronomie, June 1984, p348).

Invocation: `void palDmoon(double date, double pv[6]);`

Arguments:

date = double (Given)

TDB as a Modified Julian Date (JD-2400000.5)

pv = double [6] (Returned)

Moon x,y,z,xdot,ydot,zdot, mean equator and equinox of date (AU, AU/s)

Notes:

- Meeus quotes accuracies of 10 arcsec in longitude, 3 arcsec in latitude and 0.2 arcsec in HP (equivalent to about 20 km in distance). Comparison with JPL DE200 over the interval 1960-2025 gives RMS errors of 3.7 arcsec and 83 mas/hour in longitude, 2.3 arcsec and 48 mas/hour in latitude, 11 km and 81 mm/s in distance. The maximum errors over the same interval are 18 arcsec and 0.50 arcsec/hour in longitude, 11 arcsec and 0.24 arcsec/hour in latitude, 40 km and 0.29 m/s in distance.
- The original algorithm is expressed in terms of the obsolete timescale Ephemeris Time. Either TDB or TT can be used, but not UT without incurring significant errors (30 arcsec at the present time) due to the Moon's 0.5 arcsec/sec movement.
- The algorithm is based on pre IAU 1976 standards. However, the result has been moved onto the new (FK5) equinox, an adjustment which is in any case much smaller than the intrinsic accuracy of the procedure.
- Velocity is obtained by a complete analytical differentiation of the Meeus model.

palDrange	Normalize angle into range +/- pi	palDrange
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Description: The result is "angle" expressed in the range +/- pi. If the supplied value for "angle" is equal to +/- pi, it is returned unchanged.

Invocation: `palDrange(double angle)`

Arguments:

angle = double (Given)
The angle in radians.

palDt	Estimate the offset between dynamical time and UT	palDt
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Description: Estimate the offset between dynamical time and Universal Time for a given historical epoch.

Invocation: `double palDt(double epoch);`

Arguments:

epoch = double (Given)
Julian epoch (e.g. 1850.0)

Returned Value:

palDt = double
Rough estimate of ET-UT (after 1984, TT-UT) at the given epoch, in seconds.

Notes:

- Depending on the epoch, one of three parabolic approximations is used:

before 979 Stephenson & Morrison's 390 BC to AD 948 model 979 to 1708 Stephenson & Morrison's 948 to 1600 model after 1708 McCarthy & Babcock's post-1650 model

The breakpoints are chosen to ensure continuity: they occur at places where the adjacent models give the same answer as each other.

- The accuracy is modest, with errors of up to 20 sec during the interval since 1650, rising to perhaps 30 min by 1000 BC. Comparatively accurate values from AD 1600 are tabulated in the Astronomical Almanac (see section K8 of the 1995 AA).
- The use of double-precision for both argument and result is purely for compatibility with other SLALIB time routines.
- The models used are based on a lunar tidal acceleration value of -26.00 arcsec per century.

See Also:

Explanatory Supplement to the Astronomical Almanac, ed P.K.Seidelmann, University Science Books (1992), section 2.553, p83. This contains references to the Stephenson & Morrison and McCarthy & Babcock papers.

palDtp2s	Tangent plane to spherical coordinates	palDtp2s
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Description: Transform tangent plane coordinates into spherical.

Invocation: `palDtp2s(double xi, double eta, double raz, double decz, double *ra, double *dec);`

Arguments:

xi = double (Given)
 First rectangular coordinate on tangent plane (radians)

eta = double (Given)
 Second rectangular coordinate on tangent plane (radians)

raz = double (Given)
 RA spherical coordinate of tangent point (radians)

decz = double (Given)
 Dec spherical coordinate of tangent point (radians)

ra = double * (Returned)
 RA spherical coordinate of point to be projected (radians)

dec = double * (Returned)
 Dec spherical coordinate of point to be projected (radians)

palDtps2c	Determine RA,Dec of tangent point from coordinates	palDtps2c
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Description: From the tangent plane coordinates of a star of known RA,Dec, determine the RA,Dec of the tangent point.

Invocation: `palDtps2c(double xi, double eta, double ra, double dec, double * raz1, double decz1, double * raz2, double decz2, int *n);`

Arguments:

xi = double (Given)
 First rectangular coordinate on tangent plane (radians)

eta = double (Given)
 Second rectangular coordinate on tangent plane (radians)

ra = double (Given)
 RA spherical coordinate of star (radians)

dec = double (Given)
 Dec spherical coordinate of star (radians)

raz1 = double * (Returned)
 RA spherical coordinate of tangent point, solution 1 (radians)

decz1 = double * (Returned)
 Dec spherical coordinate of tangent point, solution 1 (radians)

raz2 = double * (Returned)

RA spherical coordinate of tangent point, solution 2 (radians)

decz2 = double * (Returned)

Dec spherical coordinate of tangent point, solution 2 (radians)

n = int * (Returned)

number of solutions: 0 = no solutions returned (note 2) 1 = only the first solution is useful (note 3) 2 = both solutions are useful (note 3)

Notes:

- The RAZ1 and RAZ2 values are returned in the range 0-2pi.
- Cases where there is no solution can only arise near the poles. For example, it is clearly impossible for a star at the pole itself to have a non-zero XI value, and hence it is meaningless to ask where the tangent point would have to be to bring about this combination of XI and DEC.
- Also near the poles, cases can arise where there are two useful solutions. The argument N indicates whether the second of the two solutions returned is useful. N=1 indicates only one useful solution, the usual case; under these circumstances, the second solution corresponds to the "over-the-pole" case, and this is reflected in the values of RAZ2 and DECZ2 which are returned.
- The DECZ1 and DECZ2 values are returned in the range +/-pi, but in the usual, non-pole-crossing, case, the range is +/-pi/2.
- This routine is the spherical equivalent of the routine sla_DTPV2C.

palDtt

Return offset between UTC and TT

palDtt

Description: Increment to be applied to Coordinated Universal Time UTC to give Terrestrial Time TT (formerly Ephemeris Time ET)

Invocation: `dtt = palDtt(double utc);`

Arguments:

utc = double (Given)

UTC date as a modified JD (JD-2400000.5)

Returned Value:

dtt = double

TT-UTC in seconds

Notes:

- Consider a comprehensive upgrade to use the time transformations in SOFA's time cookbook: http://www.iausofa.org/sofa_ts_c.pdf.
- See iauDat for a description of error conditions when calling this function with a time outside of the UTC range. This behaviour differs from slaDtt.

palEcmat	Form the equatorial to ecliptic rotation matrix - IAU 2006 precession model	palEcmat
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Description: The equatorial to ecliptic rotation matrix is found and returned. The matrix is in the sense $V(\text{ecl}) = \text{RMAT} * V(\text{equ})$; the equator, equinox and ecliptic are mean of date.

Invocation: `palEcmat(double date, double rmat[3][3])`

Arguments:

date = double (Given)

TT as Modified Julian Date (JD-2400000.5). The difference between TT and TDB is of the order of a millisecond or two (i.e. about 0.02 arc-seconds).

rmat = double[3][3] (Returned)

Rotation matrix

palEl2ue	Transform conventional elements into "universal" form	palEl2ue
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Description: Transform conventional osculating elements into "universal" form.

Invocation: `void palEl2ue (double date, int jform, double epoch, double orbinc,
double anode, double perih, double aorq, double e, double aorl, double dm, double
u[13], int *jstat);`

Arguments:

date = double (Given)

Epoch (TT MJD) of osculation (Note 3)

jform = int (Given)

Element set actually returned (1-3; Note 6)

epoch = double (Given)

Epoch of elements (TT MJD)

orbinc = double (Given)

inclination (radians)

anode = double (Given)

longitude of the ascending node (radians)

perih = double (Given)

longitude or argument of perihelion (radians)

aorq = double (Given)

mean distance or perihelion distance (AU)

e = double (Given)

eccentricity

aorl = double (Given)

mean anomaly or longitude (radians, JFORM=1,2 only)

dm = double (Given)

daily motion (radians, JFORM=1 only)

u = double [13] (Returned)

Universal orbital elements (Note 1) (0) combined mass (M+m) (1) total energy of the orbit (alpha) (2) reference (osculating) epoch (t0) (3-5) position at reference epoch (r0) (6-8) velocity at reference epoch (v0) (9) heliocentric distance at reference epoch (10) r0.v0 (11) date (t) (12) universal eccentric anomaly (psi) of date, approx

jstat = int * (Returned)

status: 0 = OK

- 1 = illegal JFORM
- 2 = illegal E
- 3 = illegal AORQ
- 4 = illegal DM
- 5 = numerical error

Notes:

- The "universal" elements are those which define the orbit for the purposes of the method of universal variables (see reference). They consist of the combined mass of the two bodies, an epoch, and the position and velocity vectors (arbitrary reference frame) at that epoch. The parameter set used here includes also various quantities that can, in fact, be derived from the other information. This approach is taken to avoiding unnecessary computation and loss of accuracy. The supplementary quantities are (i) alpha, which is proportional to the total energy of the orbit, (ii) the heliocentric distance at epoch, (iii) the outwards component of the velocity at the given epoch, (iv) an estimate of psi, the "universal eccentric anomaly" at a given date and (v) that date.
- The companion routine is *palUe2pv*. This takes the set of numbers that the present routine outputs and uses them to derive the object's position and velocity. A single prediction requires one call to the present routine followed by one call to *palUe2pv*; for convenience, the two calls are packaged as the routine *palPlanel*. Multiple predictions may be made by again calling the present routine once, but then calling *palUe2pv* multiple times, which is faster than multiple calls to *palPlanel*.
- DATE is the epoch of osculation. It is in the TT timescale (formerly Ephemeris Time, ET) and is a Modified Julian Date (JD-2400000.5).
- The supplied orbital elements are with respect to the J2000 ecliptic and equinox. The position and velocity parameters returned in the array U are with respect to the mean equator and equinox of epoch J2000, and are for the perihelion prior to the specified epoch.
- The universal elements returned in the array U are in canonical units (solar masses, AU and canonical days).
- Three different element-format options are available:

Option JFORM=1, suitable for the major planets:

Option JFORM=2, suitable for minor planets:

Option JFORM=3, suitable for comets:

- Unused elements (DM for JFORM=2, AORL and DM for JFORM=3) are not accessed.
- The algorithm was originally adapted from the EPHSLA program of D.H.P.Jones (private communication, 1996). The method is based on Stumpff's Universal Variables.

See Also:

Everhart & Pitkin, Am.J.Phys. 51, 712 (1983).

palEpc0	Convert an epoch into the appropriate form - 'B' or 'J'	palEpc0
----------------	--	----------------

Description: Converts a Besselian or Julian epoch to a Julian or Besselian epoch.

Invocation: `double palEpco(char k0, char k, double e);`

Arguments:

k0 = char (Given)

Form of result: 'B'=Besselian, 'J'=Julian

k = char (Given)

Form of given epoch: 'B' or 'J'.

Notes:

- The result is always either equal to or very close to the given epoch E. The routine is required only in applications where punctilious treatment of heterogeneous mixtures of star positions is necessary.
- k and k0 are case insensitive. This differs slightly from the Fortran SLA implementation.

- k and k0 are not validated. They are interpreted as follows:
 - If k0 and k are the same the result is e
 - If k0 is 'b' or 'B' and k isn't the conversion is J to B.
 - In all other cases, the conversion is B to J.

palEpv	Earth position and velocity with respect to the BCRS	palEpv
---------------	---	---------------

Description: Earth position and velocity, heliocentric and barycentric, with respect to the Barycentric Celestial Reference System.

Invocation: `void palEpv(double date, double ph[3], double vh[3], double pb[3], double vb[3]);`

Arguments:

date = double (Given)
Date, TDB Modified Julian Date (JD-2400000.5)

ph = double [3] (Returned)
Heliocentric Earth position (AU)

vh = double [3] (Returned)
Heliocentric Earth velocity (AU/day)

pb = double [3] (Returned)
Barycentric Earth position (AU)

vb = double [3] (Returned)
Barycentric Earth velocity (AU/day)

Notes:

- See iauEpv00 for details on accuracy
- Note that the status argument from iauEpv00 is ignored

palEtrms	Compute the E-terms vector	palEtrms
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Description: Computes the E-terms (elliptic component of annual aberration) vector.

Note the use of the J2000 aberration constant (20.49552 arcsec). This is a reflection of the fact that the E-terms embodied in existing star catalogues were computed from a variety of aberration constants. Rather than adopting one of the old constants the latest value is used here.

Invocation: `void palEtrms (double ep, double ev[3]);`

Arguments:

ep = double (Given)
Besselian epoch

ev = double [3] (Returned)
 E-terms as (dx,dy,dz)

See also:

- Smith, C.A. et al., 1989. Astr.J. 97, 265.
- Yallop, B.D. et al., 1989. Astr.J. 97, 274.

palEqecl	Transform from J2000.0 equatorial coordinates to ecliptic coordinates	palEqecl
-----------------	--	-----------------

Description: Transform from J2000.0 equatorial coordinates to ecliptic coordinates.

Invocation: `void palEqecl(double dr, double dd, double date, double *dl, double *db);`

Arguments:

dr = double (Given)
 J2000.0 mean RA (radians)

dd = double (Given)
 J2000.0 mean Dec (Radians)

date = double (Given)
 TT as Modified Julian Date (JD-2400000.5). The difference between TT and TDB is of the order of a millisecond or two (i.e. about 0.02 arc-seconds).

dl = double * (Returned)
 Ecliptic longitude (mean of date, IAU 1980 theory, radians)

db = double * (Returned)
 Ecliptic latitude (mean of date, IAU 1980 theory, radians)

palEqgal	Convert from J2000.0 equatorial coordinates to Galactic	palEqgal
-----------------	--	-----------------

Description: Transformation from J2000.0 equatorial coordinates to IAU 1958 galactic coordinates.

Invocation: `void palEqgal (double dr, double dd, double *dl, double *db);`

Arguments:

dr = double (Given)
 J2000.0 RA (radians)

dd = double (Given)
 J2000.0 Dec (radians)

dl = double * (Returned)
 Galactic longitude (radians).

db = double * (Returned)
 Galactic latitude (radians).

Notes:

The equatorial coordinates are J2000.0. Use the routine *palGe50* if conversion to B1950.0 'FK4' coordinates is required.

See Also:

Blaauw et al, Mon.Not.R.Astron.Soc.,121,123 (1960)

palEvp	Returns the barycentric and heliocentric velocity and position of the Earth	palEvp
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Description: Returns the barycentric and heliocentric velocity and position of the Earth at a given epoch, given with respect to a specified equinox. For information about accuracy, see the function *iauEvp00*.

Invocation: `void palEvp(double date, double deqx, double dvb[3], double dpb[3],
double dvh[3], double dph[3])`

Arguments:

date = double (Given)

TDB (loosely ET) as a Modified Julian Date (JD-2400000.5)

deqx = double (Given)

Julian epoch (e.g. 2000.0) of mean equator and equinox of the vectors returned. If $deqx \leq 0.0$, all vectors are referred to the mean equator and equinox (FK5) of epoch date.

dvb = double[3] (Returned)

Barycentric velocity (AU/s, AU)

dpb = double[3] (Returned)

Barycentric position (AU/s, AU)

dvh = double[3] (Returned)

heliocentric velocity (AU/s, AU)

dph = double[3] (Returned)

Heliocentric position (AU/s, AU)

palFk45z	Convert B1950.0 FK4 star data to J2000.0 FK5 assuming zero proper motion in the FK5 frame	palFk45z
-----------------	---	-----------------

Description: Convert B1950.0 FK4 star data to J2000.0 FK5 assuming zero proper motion in the FK5 frame (double precision)

This function converts stars from the Bessel-Newcomb, FK4 system to the IAU 1976, FK5, Fricke system, in such a way that the FK5 proper motion is zero. Because such a star has, in general, a non-zero proper motion in the FK4 system, the routine requires the epoch at which the position in the FK4 system was determined.

The method is from Appendix 2 of Ref 1, but using the constants of Ref 4.

Invocation: `palFk45z(double r1950, double d1950, double bepoch, double *r2000, double *d2000)`

Arguments:

r1950 = double (Given)
 B1950.0 FK4 RA at epoch (radians).
d1950 = double (Given)
 B1950.0 FK4 Dec at epoch (radians).
bepoch = double (Given)
 Besselian epoch (e.g. 1979.3)
r2000 = double (Returned)
 J2000.0 FK5 RA (Radians).
d2000 = double (Returned)
 J2000.0 FK5 Dec(Radians).

Notes:

- The epoch BEPOCH is strictly speaking Besselian, but if a Julian epoch is supplied the result will be affected only to a negligible extent.
- Conversion from Besselian epoch 1950.0 to Julian epoch 2000.0 only is provided for. Conversions involving other epochs will require use of the appropriate precession, proper motion, and E-terms routines before and/or after *palFk45z* is called.
- In the FK4 catalogue the proper motions of stars within 10 degrees of the poles do not embody the differential E-term effect and should, strictly speaking, be handled in a different manner from stars outside these regions. However, given the general lack of homogeneity of the star data available for routine astrometry, the difficulties of handling positions that may have been determined from astrometric fields spanning the polar and non-polar regions, the likelihood that the differential E-terms effect was not taken into account when allowing for proper motion in past astrometry, and the undesirability of a discontinuity in the algorithm, the decision has been made in this routine to include the effect of differential E-terms on the proper motions for all stars, whether polar or not. At epoch 2000, and measuring on the sky rather than in terms of dRA, the errors resulting from this simplification are less than 1 milliarcsecond in position and 1 milliarcsecond per century in proper motion.

References:

- Aoki,S., et al, 1983. *Astron.Astrophys.*, 128, 263.
- Smith, C.A. et al, 1989. "The transformation of astrometric catalog systems to the equinox J2000.0". *Astron.J.* 97, 265.
- Yallop, B.D. et al, 1989. "Transformation of mean star places from FK4 B1950.0 to FK5 J2000.0 using matrices in 6-space". *Astron.J.* 97, 274.
- Seidelmann, P.K. (ed), 1992. "Explanatory Supplement to the Astronomical Almanac", ISBN 0-935702-68-7.

palFk524 Convert J2000.0 FK5 star data to B1950.0 FK4 **palFk524**

Description: This function converts stars from the IAU 1976, FK5, Fricke system, to the Bessel-Newcomb, FK4 system. The precepts of Smith et al (Ref 1) are followed, using the implementation by Yallop et al (Ref 2) of a matrix method due to Standish. Kinoshita's development of Andoyer's post-Newcomb precession is used. The numerical constants from Seidelmann et al (Ref 3) are used canonically.

Invocation: `palFk524(double r2000, double d2000, double dr2000, double dd2000,
double p2000, double v2000, double *r1950, double *d1950, double *dr1950, double
*dd1950, double *p1950, double *v1950)`

Arguments:

r2000 = double (Given)
J2000.0 FK5 RA (radians).

d2000 = double (Given)
J2000.0 FK5 Dec (radians).

dr2000 = double (Given)
J2000.0 FK5 RA proper motion (rad/Jul.yr)

dd2000 = double (Given)
J2000.0 FK5 Dec proper motion (rad/Jul.yr)

p2000 = double (Given)
J2000.0 FK5 parallax (arcsec)

v2000 = double (Given)
J2000.0 FK5 radial velocity (km/s, +ve = moving away)

r1950 = double * (Returned)
B1950.0 FK4 RA (radians).

d1950 = double * (Returned)
B1950.0 FK4 Dec (radians).

dr1950 = double * (Returned)
B1950.0 FK4 RA proper motion (rad/Jul.yr)

dd1950 = double * (Returned)
B1950.0 FK4 Dec proper motion (rad/Jul.yr)

p1950 = double * (Returned)
B1950.0 FK4 parallax (arcsec)

v1950 = double * (Returned)
B1950.0 FK4 radial velocity (km/s, +ve = moving away)

Notes:

- The proper motions in RA are dRA/dt rather than $\cos(Dec)*dRA/dt$, and are per year rather than per century.

- Note that conversion from Julian epoch 2000.0 to Besselian epoch 1950.0 only is provided for. Conversions involving other epochs will require use of the appropriate precession, proper motion, and E-terms routines before and/or after FK524 is called.
- In the FK4 catalogue the proper motions of stars within 10 degrees of the poles do not embody the differential E-term effect and should, strictly speaking, be handled in a different manner from stars outside these regions. However, given the general lack of homogeneity of the star data available for routine astrometry, the difficulties of handling positions that may have been determined from astrometric fields spanning the polar and non-polar regions, the likelihood that the differential E-terms effect was not taken into account when allowing for proper motion in past astrometry, and the undesirability of a discontinuity in the algorithm, the decision has been made in this routine to include the effect of differential E-terms on the proper motions for all stars, whether polar or not. At epoch 2000, and measuring on the sky rather than in terms of dRA, the errors resulting from this simplification are less than 1 milliarcsecond in position and 1 milliarcsecond per century in proper motion.

References:

- Smith, C.A. et al, 1989. "The transformation of astrometric catalog systems to the equinox J2000.0". *Astron.J.* 97, 265.
- Yallop, B.D. et al, 1989. "Transformation of mean star places from FK4 B1950.0 to FK5 J2000.0 using matrices in 6-space". *Astron.J.* 97, 274.
- Seidelmann, P.K. (ed), 1992. "Explanatory Supplement to the Astronomical Almanac", ISBN 0-935702-68-7.

palFk54z	Convert a J2000.0 FK5 star position to B1950.0 FK4 assuming zero proper motion and parallax	palFk54z
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Description: This function converts star positions from the IAU 1976, FK5, Fricke system to the Bessel-Newcomb, FK4 system.

Invocation: `palFk54z(double r2000, double d2000, double bepoch, double *r1950,
double *d1950, double *dr1950, double *dd1950)`

Arguments:

- r2000 = double (Given)**
J2000.0 FK5 RA (radians).
- d2000 = double (Given)**
J2000.0 FK5 Dec (radians).
- bepoch = double (Given)**
Besselian epoch (e.g. 1950.0).
- r1950 = double * (Returned)**
B1950 FK4 RA (radians) at epoch "bepoch".

d1950 = double * (Returned)

B1950 FK4 Dec (radians) at epoch "bepoch".

dr1950 = double * (Returned)

B1950 FK4 proper motion (RA) (radians/trop.yr)).

dr1950 = double * (Returned)

B1950 FK4 proper motion (Dec) (radians/trop.yr)).

Notes:

- The proper motion in RA is dRA/dt rather than $\cos(Dec)*dRA/dt$.
- Conversion from Julian epoch 2000.0 to Besselian epoch 1950.0 only is provided for. Conversions involving other epochs will require use of the appropriate precession functions before and after this function is called.
- The FK5 proper motions, the parallax and the radial velocity are presumed zero.
- It is the intention that FK5 should be a close approximation to an inertial frame, so that distant objects have zero proper motion; such objects have (in general) non-zero proper motion in FK4, and this function returns those fictitious proper motions.
- The position returned by this function is in the B1950 reference frame but at Besselian epoch BEPOCH. For comparison with catalogues the "bepoch" argument will frequently be 1950.0.

palGaleq Convert from galactic to J2000.0 equatorial coordinates **palGaleq**

Description: Transformation from IAU 1958 galactic coordinates to J2000.0 equatorial coordinates.

Invocation: `void palGaleq (double dl, double db, double *dr, double *dd);`

Arguments:

dl = double (Given)

Galactic longitude (radians).

db = double (Given)

Galactic latitude (radians).

```
dr = double * (Returned)
```

J2000.0 RA (radians)

dd = double * (Returned)

J2000.0 Dec (radians)

Notes:

The equatorial coordinates are J2000.0. Use the routine `palGe50` if conversion to B1950.0 'FK4' coordinates is required.

See Also:

Blaauw et al, Mon.Not.R.Astron.Soc.,121,123 (1960)

palGalsup	Convert from galactic to supergalactic coordinates	palGalsup
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Description: Transformation from IAU 1958 galactic coordinates to de Vaucouleurs supergalactic coordinates.

Invocation: `void palGalsup (double dl, double db, double *dsl, double *dsb);`

Arguments:

dl = double (Given)
Galactic longitude.

db = double (Given)
Galactic latitude.

dsl = double * (Returned)
Supergalactic longitude.

dsb = double * (Returned)
Supergalactic latitude.

See Also:

- de Vaucouleurs, de Vaucouleurs, & Corwin, Second Reference Catalogue of Bright Galaxies, U. Texas, page 8.
- Systems & Applied Sciences Corp., Documentation for the machine-readable version of the above catalogue, Contract NAS 5-26490.

(These two references give different values for the galactic longitude of the supergalactic origin. Both are wrong; the correct value is L2=137.37.)

palGe50	Transform Galactic Coordinate to B1950 FK4	palGe50
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Description: Transformation from IAU 1958 galactic coordinates to B1950.0 'FK4' equatorial coordinates.

Invocation: `palGe50(double dl, double db, double *dr, double *dd);`

Arguments:

dl = double (Given)
Galactic longitude (radians)

db = double (Given)
Galactic latitude (radians)

dr = double * (Returned)
B9150.0 FK4 RA.

dd = double * (Returned)
B1950.0 FK4 Dec.

Notes:

- The equatorial coordinates are B1950.0 'FK4'. Use the routine *palGaleq* if conversion to J2000.0 coordinates is required.

See Also:

- Blaauw et al, Mon.Not.R.Astron.Soc.,121,123 (1960)

palGeoc	Convert geodetic position to geocentric	palGeoc
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Description: Convert geodetic position to geocentric.

Invocation: `void palGeoc(double p, double h, double * r, double *z);`

Arguments:

- p = double (Given)**
 latitude (radians)
- h = double (Given)**
 height above reference spheroid (geodetic, metres)
- r = double * (Returned)**
 distance from Earth axis (AU)
- z = double * (Returned)**
 distance from plane of Earth equator (AU)

Notes:

- Geocentric latitude can be obtained by evaluating `atan2(z,r)`
- Uses WGS84 reference ellipsoid and calls `iauGd2gc`

palIntin	Convert free-format input into an integer	palIntin
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Description: Extracts a number from an input string starting at the specified index.

Invocation: `void palIntin(const char * string, int *nstrt, long *ireslt, int *jflag);`

Arguments:

- string = const char * (Given)**
 String containing number to be decoded.
- nstrt = int * (Given and Returned)**
 Character number indicating where decoding should start. On output its value is updated to be the location of the possible next value. For compatibility with SLA the first character is index 1.

ireslt = long * (Returned)

Result. Not updated when jflag=1.

jflag = int * (Returned)

status: -1 = -OK, 0 = +OK, 1 = null, 2 = error

Notes:

- Uses the strtol() system call to do the parsing. This may lead to subtle differences when compared to the SLA/F parsing.
- Commas are recognized as a special case and are skipped if one happens to be the next character when updating nstrt. Additionally the output nstrt position will skip past any trailing space.
- If no number can be found flag will be set to 1.
- If the number overflows or underflows jflag will be set to 2. For overflow the returned result will have the value LONG_MAX, for underflow it will have the value LONG_MIN.

palMap	Convert star RA,Dec from mean place to geocentric apparent	palMap
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Description: Convert star RA,Dec from mean place to geocentric apparent.

Invocation: `void palMap(double rm, double dm, double pr, double pd, double px,
 double rv, double eq, double date, double *ra, double *da);`

Arguments:

rm = double (Given)

Mean RA (radians)

dm = double (Given)

Mean declination (radians)

pr = double (Given)

RA proper motion, changes per Julian year (radians)

pd = double (Given)

Dec proper motion, changes per Julian year (radians)

px = double (Given)

Parallax (arcsec)

rv = double (Given)

Radial velocity (km/s, +ve if receding)

eq = double (Given)

Epoch and equinox of star data (Julian)

date = double (Given)

TDB for apparent place (JD-2400000.5)

ra = double * (Returned)

Apparent RA (radians)

Notes:

- Calls palMappa and palMapqk
- The reference systems and timescales used are IAU 2006.

- For date, the distinction between the required TDB and TT is always negligible. Moreover, for all but the most critical applications UTC is adequate.
- The vector amprms(1-3) is referred to the mean equinox and equator of epoch eq.
- The parameters amprms produced by this function are used by palAmpqk, palMapqk and palMapqkz.

palMapqk	Quick mean to apparent place	palMapqk
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Description: Quick mean to apparent place: transform a star RA,Dec from mean place to geocentric apparent place, given the star-independent parameters.

Use of this routine is appropriate when efficiency is important and where many star positions, all referred to the same equator and equinox, are to be transformed for one epoch. The star-independent parameters can be obtained by calling the *palMappa* routine.

If the parallax and proper motions are zero the *palMapqkz* routine can be used instead.

Invocation: `void palMapqk (double rm, double dm, double pr, double pd, double px, double rv, double amprms[21], double *ra, double *da);`

Arguments:

rm = double (Given)

Mean RA (radians)

dm = double (Given)

Mean declination (radians)

pr = double (Given)

RA proper motion, changes per Julian year (radians)

pd = double (Given)

Dec proper motion, changes per Julian year (radians)

px = double (Given)

Parallax (arcsec)

rv = double (Given)

Radial velocity (km/s, +ve if receding)

amprms = double [21] (Given)

Star-independent mean-to-apparent parameters (see *palMappa*).

ra = double * (Returned)

Apparent RA (radians)

dec = double * (Returned)

Apparent dec (radians)

Notes:

- The reference frames and timescales used are post IAU 2006.

palMapqkz	Quick mean to apparent place	palMapqkz
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Description: Quick mean to apparent place: transform a star RA,dec from mean place to geocentric apparent place, given the star-independent parameters, and assuming zero parallax and proper motion.

Use of this function is appropriate when efficiency is important and where many star positions, all with parallax and proper motion either zero or already allowed for, and all

referred to the same equator and equinox, are to be transformed for one epoch. The star-independent parameters can be obtained by calling the *palMappa* function.

The corresponding function for the case of non-zero parallax and proper motion is *palMapqk*.

The reference systems and timescales used are IAU 2006.

Strictly speaking, the function is not valid for solar-system sources, though the error will usually be extremely small.

Invocation: `void palMapqkz(double rm, double dm, double amprms[21], double *ra, double *da)`

Arguments:

rm = double (Given)

Mean RA (radians).

dm = double (Given)

Mean Dec (radians).

amprms = double[21] (Given)

Star-independent mean-to-apparent parameters (see *palMappa*): (0-3) not used (4-6) not used (7) not used (8-10) abv: barycentric Earth velocity in units of c (11) $\sqrt{1-v^2}$ where $v=\text{modulus}(\text{abv})$ (12-20) precession/nutation (3,3) matrix

ra = double * (Returned)

Apparent RA (radians).

da = double * (Returned)

Apparent Dec (radians).

palNut	Form the matrix of nutation	palNut
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Description: Form the matrix of nutation for a given date using the IAU 2006 nutation model and *palDeuler*.

Invocation: `void palNut(double date, double rmatn[3][3]);`

Arguments:

date = double (Given)

TT as modified Julian date (JD-2400000.5)

rmatn = double [3][3] (Returned)

Nutation matrix in the sense $v(\text{true}) = \text{rmatn} * v(\text{mean})$ where $v(\text{true})$ is the star vector relative to the true equator and equinox of date and $v(\text{mean})$ is the star vector relative to the mean equator and equinox of date.

Notes:

- Uses *iauNut06a* via *palNutc*
- The distinction between TDB and TT is negligible. For all but the most critical applications UTC is adequate.

palNutc	Calculate nutation longitude & obliquity components	palNutc
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Description: Calculates the longitude * obliquity components and mean obliquity using the SOFA library.

Invocation: `void palNutc(double date, double * dpsi, double *deps, double *eps0);`

Arguments:

date = double (Given)
 TT as modified Julian date (JD-2400000.5)

dpsi = double * (Returned)
 Nutation in longitude

deps = double * (Returned)
 Nutation in obliquity

eps0 = double * (Returned)
 Mean obliquity.

Notes:

- Calls iauObl06 and iauNut06a and therefore uses the IAU 206 precession/nutation model.
- Note the change from SLA/F regarding the date. TT is used rather than TDB.

palObs	Parameters of selected ground-based observing stations	palObs
---------------	--	---------------

Description: Station numbers, identifiers, names and other details are subject to change and should not be hardwired into application programs.

All characters in "c" up to the first space are checked; thus an abbreviated ID will return the parameters for the first station in the list which matches the abbreviation supplied, and no station in the list will ever contain embedded spaces. "c" must not have leading spaces.

IMPORTANT – BEWARE OF THE LONGITUDE SIGN CONVENTION. The longitude returned by sla_OBS is west-positive in accordance with astronomical usage. However, this sign convention is left-handed and is the opposite of the one used by geographers; elsewhere in PAL the preferable east-positive convention is used. In particular, note that for use in palAop, palAoppa and palOap the sign of the longitude must be reversed.

Users are urged to inform the author of any improvements they would like to see made. For example:

typographical corrections more accurate parameters better station identifiers or names additional stations

Invocation: `int palObs(size_t n, const char * c, char * ident, size_t identlen,
char * name, size_t namelen, double * w, double * p, double * h);`

Arguments:

n = size_t (Given)

Number specifying the observing station. If 0 the identifier in "c" is used to determine the observing station to use.

c = const char * (Given)

Identifier specifying the observing station for which the parameters should be returned. Only used if n is 0. Can be NULL for n>0. Case insensitive.

ident = char * (Returned)

Identifier of the observing station selected. Will be identical to "c" if n==0. Unchanged if "n" or "c" do not match an observing station. Should be at least 11 characters (including the trailing nul).

identlen = size_t (Given)

Size of the buffer "ident" including trailing nul.

name = char * (Returned)

Full name of the specified observing station. Contains "?" if "n" or "c" did not correspond to a valid station. Should be at least 41 characters (including the trailing nul).

w = double * (Returned)

Longitude (radians, West +ve). Unchanged if observing station could not be identified.

p = double * (Returned)

Geodetic latitude (radians, North +ve). Unchanged if observing station could not be identified.

h = double * (Returned)

Height above sea level (metres). Unchanged if observing station could not be identified.

Returned Value:

palObs = int

0 if an observing station was returned. -1 if no match was found.

Notes:

- Differs from the SLA interface in that the output short name is not the same variable as the input short name. This simplifies consting. Additionally the size of the output buffers are now specified in the API and a status integer is returned.

palPa

HA, Dec to Parallactic Angle

palPa

Description: Converts HA, Dec to Parallactic Angle.

Invocation: `double palPa(double ha, double dec, double phi);`

Arguments:

ha = double (Given)
 Hour angle in radians (Geocentric apparent)

dec = double (Given)
 Declination in radians (Geocentric apparent)

phi = double (Given)
 Observatory latitude in radians (geodetic)

Returned Value:

palPa = double
 Parallax angle in the range -pi to +pi.

Notes:

- The parallactic angle at a point in the sky is the position angle of the vertical, i.e. the angle between the direction to the pole and to the zenith. In precise applications care must be taken only to use geocentric apparent HA,Dec and to consider separately the effects of atmospheric refraction and telescope mount errors.
- At the pole a zero result is returned.

palPertel	Update elements by applying planetary perturbations	palPertel
------------------	---	------------------

Description: Update the osculating orbital elements of an asteroid or comet by applying planetary perturbations.

Invocation: `void palPertel (int jform, double date0, double date1, double epoch0, double orbi0, double anode0, double perih0, double aorq0, double e0, double am0, double *epoch1, double *orbi1, double *anode1, double *perih1, double *aorq1, double *e1, double *am1, int *jstat);`

Arguments:

jform = int (Given)
 Element set actually returned (1-3; Note 6)

date0 = double (Given)
 Date of osculation (TT MJD) for the given elements.

date1 = double (Given)
 Date of osculation (TT MJD) for the updated elements.

epoch0 = double (Given)
 Epoch of elements (TT MJD)

orbi0 = double (Given)
 inclination (radians)

anode0 = double (Given)
 longitude of the ascending node (radians)

perih0 = double (Given)
 longitude or argument of perihelion (radians)
aorq0 = double (Given)
 mean distance or perihelion distance (AU)
e0 = double (Given)
 eccentricity
am0 = double (Given)
 mean anomaly (radians, JFORM=2 only)
epoch1 = double * (Returned)
 Epoch of elements (TT MJD)
orbi1 = double * (Returned)
 inclination (radians)
anode1 = double * (Returned)
 longitude of the ascending node (radians)
perih1 = double * (Returned)
 longitude or argument of perihelion (radians)
aorq1 = double * (Returned)
 mean distance or perihelion distance (AU)
e1 = double * (Returned)
 eccentricity
am1 = double * (Returned)
 mean anomaly (radians, JFORM=2 only)
jstat = int * (Returned)
 status:

- +102 = warning, distant epoch
- +101 = warning, large timespan (> 100 years)
- +1 to +10 = coincident with planet (Note 6)
- 0 = OK
- -1 = illegal JFORM
- -2 = illegal E0
- -3 = illegal AORQ0
- -4 = internal error
- -5 = numerical error

Notes:

- Two different element-format options are available:

Option JFORM=2, suitable for minor planets:

EPOCH = epoch of elements (TT MJD) ORBI = inclination *i* (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = mean distance, *a* (AU) E = eccentricity, *e* AM = mean anomaly *M* (radians)

Option JFORM=3, suitable for comets:

EPOCH = epoch of perihelion (TT MJD) ORBI = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = perihelion distance, q (AU) E = eccentricity, e

- DATE0, DATE1, EPOCH0 and EPOCH1 are all instants of time in the TT timescale (formerly Ephemeris Time, ET), expressed as Modified Julian Dates (JD-2400000.5).

DATE0 is the instant at which the given (i.e. unperturbed) osculating elements are correct.

DATE1 is the specified instant at which the updated osculating elements are correct.

EPOCH0 and EPOCH1 will be the same as DATE0 and DATE1 (respectively) for the JFORM=2 case, normally used for minor planets. For the JFORM=3 case, the two epochs will refer to perihelion passage and so will not, in general, be the same as DATE0 and/or DATE1 though they may be similar to one another.

- The elements are with respect to the J2000 ecliptic and equinox.
- Unused elements (AM0 and AM1 for JFORM=3) are not accessed.
- See the *palPertue* routine for details of the algorithm used.
- This routine is not intended to be used for major planets, which is why JFORM=1 is not available and why there is no opportunity to specify either the longitude of perihelion or the daily motion. However, if JFORM=2 elements are somehow obtained for a major planet and supplied to the routine, sensible results will, in fact, be produced. This happens because the *sla_PERTUE* routine that is called to perform the calculations checks the separation between the body and each of the planets and interprets a suspiciously small value (0.001 AU) as an attempt to apply it to the planet concerned. If this condition is detected, the contribution from that planet is ignored, and the status is set to the planet number (1-10 = Mercury, Venus, EMB, Mars, Jupiter, Saturn, Uranus, Neptune, Earth, Moon) as a warning.

See Also:

- Sterne, Theodore E., "An Introduction to Celestial Mechanics", Interscience Publishers Inc., 1960. Section 6.7, p199.

palPertue Update the universal elements by applying **palPertue**
 planetary perturbations

Description: Update the universal elements of an asteroid or comet by applying planetary perturbations.

Invocation: `void palPertue(double date, double u[13], int *jstat);`

Arguments:

date = double (Given)

Final epoch (TT MJD) for the update elements.

u = const double [13] (Given & Returned)

Universal orbital elements (Note 1) (0) combined mass (M+m) (1) total energy of the orbit (alpha) (2) reference (osculating) epoch (t0) (3-5) position at reference epoch (r0) (6-8) velocity at reference epoch (v0) (9) heliocentric distance at reference epoch (10) r0.v0 (11) date (t) (12) universal eccentric anomaly (psi) of date, approx

jstat = int * (Returned)

status: +102 = warning, distant epoch +101 = warning, large timespan (> 100 years) +1 to +10 = coincident with major planet (Note 5) 0 = OK

- 1 = numerical error

Notes:

- The "universal" elements are those which define the orbit for the purposes of the method of universal variables (see reference 2). They consist of the combined mass of the two bodies, an epoch, and the position and velocity vectors (arbitrary reference frame) at that epoch. The parameter set used here includes also various quantities that can, in fact, be derived from the other information. This approach is taken to avoiding unnecessary computation and loss of accuracy. The supplementary quantities are (i) alpha, which is proportional to the total energy of the orbit, (ii) the heliocentric distance at epoch, (iii) the outwards component of the velocity at the given epoch, (iv) an estimate of psi, the "universal eccentric anomaly" at a given date and (v) that date.
- The universal elements are with respect to the J2000 equator and equinox.
- The epochs DATE, U(3) and U(12) are all Modified Julian Dates (JD-2400000.5).
- The algorithm is a simplified form of Encke's method. It takes as a basis the unperturbed motion of the body, and numerically integrates the perturbing accelerations from the major planets. The expression used is essentially Sterne's 6.7-2 (reference 1). Everhart and Pitkin (reference 2) suggest rectifying the orbit at each integration step by propagating the new perturbed position and velocity as the new universal variables. In the present routine the orbit is rectified less frequently than this, in order to gain a slight speed advantage. However, the rectification is done directly in terms of position and velocity, as suggested by Everhart and Pitkin, bypassing the use of conventional orbital elements.

The f(q) part of the full Encke method is not used. The purpose of this part is to avoid subtracting two nearly equal quantities when calculating the "indirect member", which takes account of the small change in the Sun's attraction due to the slightly displaced position of the perturbed body. A simpler, direct calculation in double precision proves to be faster and not significantly less accurate.

Apart from employing a variable timestep, and occasionally "rectifying the orbit" to keep the indirect member small, the integration is done in a fairly straightforward way. The acceleration estimated for the middle of the timestep is assumed to apply throughout that timestep; it is also used in the extrapolation of the perturbations to the middle of the next timestep, to predict the new disturbed position. There is no iteration within a timestep.

Measures are taken to reach a compromise between execution time and accuracy. The starting-point is the goal of achieving arcsecond accuracy for ordinary minor planets over

Invocation: `void palPlanel (double date, int jform, double epoch, double orbinc,
double anode, double perih, double aorq, double e, double aorl, double dm, double
pv[6], int *jstat);`

Arguments:

date = double (Given)

Epoch (TT MJD) of osculation (Note 1)

jform = int (Given)

Element set actually returned (1-3; Note 3)

epoch = double (Given)

Epoch of elements (TT MJD) (Note 4)

orbinc = double (Given)

inclination (radians)

anode = double (Given)

longitude of the ascending node (radians)

perih = double (Given)

longitude or argument of perihelion (radians)

aorq = double (Given)

mean distance or perihelion distance (AU)

e = double (Given)

eccentricity

aorl = double (Given)

mean anomaly or longitude (radians, JFORM=1,2 only)

dm = double (Given)

daily motion (radians, JFORM=1 only)

u = double [13] (Returned)

Universal orbital elements (Note 1) (0) combined mass (M+m) (1) total energy of the orbit (alpha) (2) reference (osculating) epoch (t0) (3-5) position at reference epoch (r0) (6-8) velocity at reference epoch (v0) (9) heliocentric distance at reference epoch (10) r0.v0 (11) date (t) (12) universal eccentric anomaly (psi) of date, approx

jstat = int * (Returned)

status: 0 = OK

- -1 = illegal JFORM
- -2 = illegal E
- -3 = illegal AORQ
- -4 = illegal DM
- -5 = numerical error

Notes:

- DATE is the instant for which the prediction is required. It is in the TT timescale (formerly Ephemeris Time, ET) and is a Modified Julian Date (JD-2400000.5).
- The elements are with respect to the J2000 ecliptic and equinox.

- A choice of three different element-set options is available:

Option JFORM = 1, suitable for the major planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = longitude of perihelion, curly pi (radians) AORQ = mean distance, a (AU) E = eccentricity, e (range 0 to <1) AORL = mean longitude L (radians) DM = daily motion (radians)

Option JFORM = 2, suitable for minor planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = mean distance, a (AU) E = eccentricity, e (range 0 to <1) AORL = mean anomaly M (radians)

Option JFORM = 3, suitable for comets:

EPOCH = epoch of elements and perihelion (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = perihelion distance, q (AU) E = eccentricity, e (range 0 to 10)

Unused arguments (DM for JFORM=2, AORL and DM for JFORM=3) are not accessed.

- Each of the three element sets defines an unperturbed heliocentric orbit. For a given epoch of observation, the position of the body in its orbit can be predicted from these elements, which are called "osculating elements", using standard two-body analytical solutions. However, due to planetary perturbations, a given set of osculating elements remains usable for only as long as the unperturbed orbit that it describes is an adequate approximation to reality. Attached to such a set of elements is a date called the "osculating epoch", at which the elements are, momentarily, a perfect representation of the instantaneous position and velocity of the body.

Therefore, for any given problem there are up to three different epochs in play, and it is vital to distinguish clearly between them:

- . The epoch of observation: the moment in time for which the position of the body is to be predicted.
- . The epoch defining the position of the body: the moment in time at which, in the absence of perturbations, the specified position (mean longitude, mean anomaly, or perihelion) is reached.
- . The osculating epoch: the moment in time at which the given elements are correct.

For the major-planet and minor-planet cases it is usual to make the epoch that defines the position of the body the same as the epoch of osculation. Thus, only two different epochs are involved: the epoch of the elements and the epoch of observation.

For comets, the epoch of perihelion fixes the position in the orbit and in general a different epoch of osculation will be chosen. Thus, all three types of epoch are involved.

For the present routine:

- . The epoch of observation is the argument DATE.
- . The epoch defining the position of the body is the argument EPOCH.

. The osculating epoch is not used and is assumed to be close enough to the epoch of observation to deliver adequate accuracy. If not, a preliminary call to `sla_PERTEL` may be used to update the element-set (and its associated osculating epoch) by applying planetary perturbations.

- The reference frame for the result is with respect to the mean equator and equinox of epoch J2000.
- The algorithm was originally adapted from the EPHSLA program of D.H.P.Jones (private communication, 1996). The method is based on Stumpff's Universal Variables.

See Also:

Everhart, E. & Pitkin, E.T., Am.J.Phys. 51, 712, 1983.

palPlanet	Approximate heliocentric position and velocity of major planet	palPlanet
------------------	---	------------------

Description: Calculates the approximate heliocentric position and velocity of the specified major planet.

Invocation: `void palPlanet (double date, int np, double pv[6], int *j);`

Arguments:

date = double (Given)

TDB Modified Julian Date (JD-2400000.5).

np = int (Given)

planet (1=Mercury, 2=Venus, 3=EMB, 4=Mars, 5=Jupiter, 6=Saturn, 7=Uranus, 8=Neptune)

pv = double [6] (Returned)

heliocentric x,y,z,xdot,ydot,zdot, J2000, equatorial triad in units AU and AU/s.

j = int * (Returned)

- -2 = solution didn't converge.
- -1 = illegal np (1-8)
- 0 = OK
- +1 = warning: year outside 1000-3000

Notes:

- See SOFA `iauPlan94` for details
- Note that Pluto is supported in SLA/F but not in this routine
- Status -2 is equivalent to `iauPlan94` status +2.
- Note that velocity units here match the SLA/F documentation.

```

date = double (Given)
    TT MJD of observation (JD-2400000.5)

elong = double (Given)
    Observer's east longitude (radians)

phi = double (Given)
    Observer's geodetic latitude (radians)

jform = int (Given)
    Element set actually returned (1-3; Note 6)

epoch = double (Given)
    Epoch of elements (TT MJD)

orbinc = double (Given)
    inclination (radians)

anode = double (Given)
    longitude of the ascending node (radians)

perih = double (Given)
    longitude or argument of perihelion (radians)

aorq = double (Given)
    mean distance or perihelion distance (AU)

e = double (Given)
    eccentricity

aorl = double (Given)
    mean anomaly or longitude (radians, JFORM=1,2 only)

dm = double (Given)
    daily motion (radians, JFORM=1 only)

ra = double * (Returned)
    Topocentric apparent RA (radians)

dec = double * (Returned)
    Topocentric apparent Dec (radians)

r = double * (Returned)
    Distance from observer (AU)

jstat = int * (Returned)
    status: 0 = OK

```

- -1 = illegal jform
- -2 = illegal e
- -3 = illegal aorq
- -4 = illegal dm
- -5 = numerical error

Notes:

- DATE is the instant for which the prediction is required. It is in the TT timescale (formerly Ephemeris Time, ET) and is a Modified Julian Date (JD-2400000.5).
- The longitude and latitude allow correction for geocentric parallax. This is usually a small effect, but can become important for near-Earth asteroids. Geocentric positions can be generated by appropriate use of routines *palEpv* (or *palEvp*) and *palUe2pv*.
- The elements are with respect to the J2000 ecliptic and equinox.
- A choice of three different element-set options is available:

Option JFORM = 1, suitable for the major planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = longitude of perihelion, curly pi (radians) AORQ = mean distance, a (AU) E = eccentricity, e (range 0 to <1) AORL = mean longitude L (radians) DM = daily motion (radians)

Option JFORM = 2, suitable for minor planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = mean distance, a (AU) E = eccentricity, e (range 0 to <1) AORL = mean anomaly M (radians)

Option JFORM = 3, suitable for comets:

EPOCH = epoch of elements and perihelion (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = perihelion distance, q (AU) E = eccentricity, e (range 0 to 10)

Unused arguments (DM for JFORM=2, AORL and DM for JFORM=3) are not accessed.

- Each of the three element sets defines an unperturbed heliocentric orbit. For a given epoch of observation, the position of the body in its orbit can be predicted from these elements, which are called "osculating elements", using standard two-body analytical solutions. However, due to planetary perturbations, a given set of osculating elements remains usable for only as long as the unperturbed orbit that it describes is an adequate approximation to reality. Attached to such a set of elements is a date called the "osculating epoch", at which the elements are, momentarily, a perfect representation of the instantaneous position and velocity of the body.

Therefore, for any given problem there are up to three different epochs in play, and it is vital to distinguish clearly between them:

- . The epoch of observation: the moment in time for which the position of the body is to be predicted.
- . The epoch defining the position of the body: the moment in time at which, in the absence of perturbations, the specified position (mean longitude, mean anomaly, or perihelion) is reached.
- . The osculating epoch: the moment in time at which the given elements are correct.

For the major-planet and minor-planet cases it is usual to make the epoch that defines the position of the body the same as the epoch of osculation. Thus, only two different epochs are involved: the epoch of the elements and the epoch of observation.

For comets, the epoch of perihelion fixes the position in the orbit and in general a different epoch of osculation will be chosen. Thus, all three types of epoch are involved.

For the present routine:

- . The epoch of observation is the argument DATE.
- . The epoch defining the position of the body is the argument EPOCH.
- . The osculating epoch is not used and is assumed to be close enough to the epoch of observation to deliver adequate accuracy. If not, a preliminary call to `sla_PERTEL` may be used to update the element-set (and its associated osculating epoch) by applying planetary perturbations.
 - Two important sources for orbital elements are Horizons, operated by the Jet Propulsion Laboratory, Pasadena, and the Minor Planet Center, operated by the Center for Astrophysics, Harvard.

The JPL Horizons elements (heliocentric, J2000 ecliptic and equinox) correspond to SLALIB arguments as follows.

Major planets:

JFORM = 1 EPOCH = JDCT-2400000.5 ORBINC = IN (in radians) ANODE = OM (in radians) PERIH = OM+W (in radians) AORQ = A E = EC AORL = MA+OM+W (in radians) DM = N (in radians)

Epoch of osculation = JDCT-2400000.5

Minor planets:

JFORM = 2 EPOCH = JDCT-2400000.5 ORBINC = IN (in radians) ANODE = OM (in radians) PERIH = W (in radians) AORQ = A E = EC AORL = MA (in radians)

Epoch of osculation = JDCT-2400000.5

Comets:

JFORM = 3 EPOCH = Tp-2400000.5 ORBINC = IN (in radians) ANODE = OM (in radians) PERIH = W (in radians) AORQ = QR E = EC

Epoch of osculation = JDCT-2400000.5

The MPC elements correspond to SLALIB arguments as follows.

Minor planets:

JFORM = 2 EPOCH = Epoch-2400000.5 ORBINC = Incl. (in radians) ANODE = Node (in radians) PERIH = Perih. (in radians) AORQ = a E = e AORL = M (in radians)

Epoch of osculation = Epoch-2400000.5

Comets:

JFORM = 3 EPOCH = T-2400000.5 ORBINC = Incl. (in radians) ANODE = Node. (in radians) PERIH = Perih. (in radians) AORQ = q E = e

Epoch of osculation = Epoch-2400000.5

palPlantu Topocentric RA,Dec of a Solar-System object **palPlantu** from universal elements

Description: Topocentric apparent RA,Dec of a Solar-System object whose heliocentric universal elements are known.

Invocation: `void palPlantu (double date, double elong, double phi, const double u[13], double *ra, double *dec, double *r, int *jstat) {`

Arguments:

date = double (Given)

TT MJD of observation (JD-2400000.5)

elong = double (Given)

Observer's east longitude (radians)

phi = double (Given)

Observer's geodetic latitude (radians)

u = const double [13] (Given)

Universal orbital elements

- (0) combined mass (M+m)
- (1) total energy of the orbit (alpha)
- (2) reference (osculating) epoch (t0)
- (3-5) position at reference epoch (r0)
- (6-8) velocity at reference epoch (v0)
- (9) heliocentric distance at reference epoch
- (10) r0.v0
- (11) date (t)
- (12) universal eccentric anomaly (psi) of date, approx

ra = double * (Returned)

Topocentric apparent RA (radians)

dec = double * (Returned)

Topocentric apparent Dec (radians)

r = double * (Returned)

Distance from observer (AU)

jstat = int * (Returned)

status: 0 = OK

- -1 = radius vector zero
- -2 = failed to converge

Notes:

- DATE is the instant for which the prediction is required. It is in the TT timescale (formerly Ephemeris Time, ET) and is a Modified Julian Date (JD-2400000.5).
- The longitude and latitude allow correction for geocentric parallax. This is usually a small effect, but can become important for near-Earth asteroids. Geocentric positions can be generated by appropriate use of routines *palEpv* (or *palEvp*) and *palUe2pv*.
- The "universal" elements are those which define the orbit for the purposes of the method of universal variables (see reference 2). They consist of the combined mass of the two bodies, an epoch, and the position and velocity vectors (arbitrary reference frame) at that epoch. The parameter set used here includes also various quantities that can, in fact, be derived from the other information. This approach is taken to avoiding unnecessary computation and loss of accuracy. The supplementary quantities are (i) alpha, which is proportional to the total energy of the orbit, (ii) the heliocentric distance at epoch, (iii) the outwards component of the velocity at the given epoch, (iv) an estimate of psi, the "universal eccentric anomaly" at a given date and (v) that date.
- The universal elements are with respect to the J2000 equator and equinox.

See Also:

- Sterne, Theodore E., "An Introduction to Celestial Mechanics", Interscience Publishers Inc., 1960. Section 6.7, p199.
- Everhart, E. & Pitkin, E.T., Am.J.Phys. 51, 712, 1983.

palPm Apply corrections for proper motion a star RA,Dec **palPm**

Description: Apply corrections for proper motion to a star RA,Dec using the SOFA routine *iauStarpm*.

Invocation: `void palPm (double r0, double d0, double pr, double pd, double px,
double rv, double ep0, double ep1, double *r1, double *d1);`

Arguments:

r0 = double (Given)
RA at epoch ep0 (radians)

d0 = double (Given)
Dec at epoch ep0 (radians)

pr = double (Given)
RA proper motion in radians per year.

pd = double (Given)
Dec proper motion in radians per year.

px = double (Given)
Parallax (arcsec)

Notes:

- Uses `iauStarpmp` but ignores the status returns from that routine. In particular note that parallax should not be zero when the proper motions are non-zero. SLA/F allows parallax to be zero.
- Assumes all epochs are Julian epochs.

Kinoshita, H. (1975) 'Formulas for precession', SAO Special Report No. 364, Smithsonian Institution Astrophysical Observatory, Cambridge, Massachusetts.

```

sys = const char [3] (Given)
    Precession to be applied: FK4 or FK5. Case insensitive.

ep0 = double (Given)
    Starting epoch.

ep1 = double (Given)
    Ending epoch

ra = double * (Given & Returned)
    On input the RA mean equator & equinox at epoch ep0. On exit the RA mean
    equator & equinox of epoch ep1.

dec = double * (Given & Returned)
    On input the dec mean equator & equinox at epoch ep0. On exit the dec mean
    equator & equinox of epoch ep1.

```

- Uses palPrec for FK5 data and palPrebn for FK4 data.
- The epochs are Besselian if SYSTEM='FK4' and Julian if 'FK5'. For example, to precess coordinates in the old system from equinox 1900.0 to 1950.0 the call would be: palPreces("FK4", 1900.0, 1950.0, &ra, &dc);
- This routine will NOT correctly convert between the old and the new systems - for example conversion from B1950 to J2000. For these purposes see palFk425, palFk524, palFk45z and palFk54z.
- If an invalid SYSTEM is supplied, values of -99D0,-99D0 will be returned for both RA and DC.

Description: Form the matrix of bias-precession-nutation (IAU 2006/2000A). The epoch and date are TT (but TDB is usually close enough). The matrix is in the sense $\mathbf{v}(\text{true}) = \mathbf{rmatpn} * \mathbf{v}(\text{mean})$.

Arguments:

Julian epoch for mean coordinates.

Modified Julian Date (JD-2400000.5) for true coordinates.

combined NPB matrix

Description: Heliocentric osculating elements obtained from instantaneous position and velocity.

Arguments:

Heliocentric x,y,z,xdot,ydot,zdot of date, J2000 equatorial triad (AU,AU/s; Note 1)

Date (TT Modified Julian Date = JD-2400000.5)

pmass = double (Given)
 Mass of the planet (Sun=1; Note 2)
jformr = int (Given)
 Requested element set (1-3; Note 3)
jform = int * (Returned)
 Element set actually returned (1-3; Note 4)
epoch = double * (Returned)
 Epoch of elements (TT MJD)
orbinc = double * (Returned)
 inclination (radians)
anode = double * (Returned)
 longitude of the ascending node (radians)
perih = double * (Returned)
 longitude or argument of perihelion (radians)
aorq = double * (Returned)
 mean distance or perihelion distance (AU)
e = double * (Returned)
 eccentricity
aorl = double * (Returned)
 mean anomaly or longitude (radians, JFORM=1,2 only)
dm = double * (Returned)
 daily motion (radians, JFORM=1 only)
jstat = int * (Returned)
 status: 0 = OK
 • -1 = illegal PMASS
 • -2 = illegal JFORMR
 • -3 = position/velocity out of range

Notes:

- The PV 6-vector is with respect to the mean equator and equinox of epoch J2000. The orbital elements produced are with respect to the J2000 ecliptic and mean equinox.
- The mass, PMASS, is important only for the larger planets. For most purposes (e.g. asteroids) use 0D0. Values less than zero are illegal.
- Three different element-format options are supported:

Option JFORM=1, suitable for the major planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = longitude of perihelion, curly pi (radians) AORQ = mean distance, a (AU) E = eccentricity, e AORL = mean longitude L (radians) DM = daily motion (radians)

Option JFORM=2, suitable for minor planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = mean distance, a (AU) E = eccentricity, e AORL = mean anomaly M (radians)

Option JFORM=3, suitable for comets:

EPOCH = epoch of perihelion (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = perihelion distance, q (AU) E = eccentricity, e

- It may not be possible to generate elements in the form requested through JFORMR. The caller is notified of the form of elements actually returned by means of the JFORM argument:

JFORMR JFORM meaning

1 1 OK - elements are in the requested format 1 2 never happens 1 3 orbit not elliptical
 2 1 never happens 2 2 OK - elements are in the requested format 2 3 orbit not elliptical
 3 1 never happens 3 2 never happens 3 3 OK - elements are in the requested format

- The arguments returned for each value of JFORM (cf Note 5: JFORM may not be the same as JFORMR) are as follows:

JFORM 1 2 3 EPOCH t0 t0 T ORBINC i i i ANODE Omega Omega Omega PERIH curly pi
 omega omega AORQ a a q E e e e AORL L M - DM n - -

where:

t0 is the epoch of the elements (MJD, TT) T " epoch of perihelion (MJD, TT) i " inclination (radians) Omega " longitude of the ascending node (radians) curly pi " longitude of perihelion (radians) omega " argument of perihelion (radians) a " mean distance (AU) q " perihelion distance (AU) e " eccentricity L " longitude (radians, 0-2pi) M " mean anomaly (radians, 0-2pi) n " daily motion (radians)

- means no value is set
- At very small inclinations, the longitude of the ascending node ANODE becomes indeterminate and under some circumstances may be set arbitrarily to zero. Similarly, if the orbit is close to circular, the true anomaly becomes indeterminate and under some circumstances may be set arbitrarily to zero. In such cases, the other elements are automatically adjusted to compensate, and so the elements remain a valid description of the orbit.
- The osculating epoch for the returned elements is the argument DATE.
- Reference: Sterne, Theodore E., "An Introduction to Celestial Mechanics", Interscience Publishers, 1960

palPv2ue Universal elements to position and velocity **palPv2ue**

Description: Construct a universal element set based on an instantaneous position and velocity.

Invocation: `void palPv2ue(const double pv[6], double date, double pmass, double u[13], int * jstat);`

Arguments:

pv = double [6] (Given)

Heliocentric x,y,z,xdot,ydot,zdot of date, (AU,AU/s; Note 1)

date = double (Given)

Date (TT modified Julian Date = JD-2400000.5)

pmass = double (Given)

Mass of the planet (Sun=1; note 2)

u = double [13] (Returned)

Universal orbital elements (Note 3)

- (0) combined mass (M+m)
- (1) total energy of the orbit (alpha)
- (2) reference (osculating) epoch (t0)
- (3-5) position at reference epoch (r0)
- (6-8) velocity at reference epoch (v0)
- (9) heliocentric distance at reference epoch
- (10) r0.v0
- (11) date (t)
- (12) universal eccentric anomaly (psi) of date, approx

jstat = int * (Returned)

status: 0 = OK

- -1 = illegal PMASS
- -2 = too close to Sun
- -3 = too slow

Notes:

- The PV 6-vector can be with respect to any chosen inertial frame, and the resulting universal-element set will be with respect to the same frame. A common choice will be mean equator and ecliptic of epoch J2000.
- The mass, PMASS, is important only for the larger planets. For most purposes (e.g. asteroids) use 0D0. Values less than zero are illegal.
- The "universal" elements are those which define the orbit for the purposes of the method of universal variables (see reference). They consist of the combined mass of the two bodies, an epoch, and the position and velocity vectors (arbitrary reference frame) at that epoch. The parameter set used here includes also various quantities

- Reference: Everhart, E. & Pitkin, E.T., Am.J.Phys. 51, 712, 1983.

- The WGS84 reference ellipsoid is used.

```

date = double (Given)
    MJD of observation (JD-2400000.5) in TDB. For all practical purposes TT can be
    used instead of TDB, and for many applications UT will do (except for the Moon).

np = int (Given)
    Planet: 1 = Mercury 2 = Venus 3 = Moon 4 = Mars 5 = Jupiter 6 = Saturn 7 =
    Uranus 8 = Neptune else = Sun

```


Notes:

- Unlike with `slaRdplan`, Pluto is not supported.
- The longitude and latitude allow correction for geocentric parallax. This is a major effect for the Moon, but in the context of the limited accuracy of the present routine its effect on planetary positions is small (negligible for the outer planets). Geocentric positions can be generated by appropriate use of the routines `palDmoon` and `iauPlan94`.

palRverot Velocity component in a given direction due to Earth rotation **palRverot**

The simple algorithm used assumes a spherical Earth, of a radius chosen to give results accurate to about 0.0005 km/s for observing stations at typical latitudes and heights. For applications requiring greater precision, use the routine `palPvobs`.

Arguments:

Returned Value:

palRverot = double
 Component of Earth rotation in direction RA,DA (km/s). The result is +ve when the observatory is receding from the given point on the sky.

$$\mathbf{r2000} = \text{double}(\mathbf{Given})$$

J2000.0 mean RA (radians)

d2000 = double (Given)
 J2000.0 mean Dec (radians)

Returned Value:

Component of SOLAR motion in direction R2000,D2000 (km/s).

Reference:

- IAU Trans 1976, 168, p201.

palRvlsrd Velocity component in a given direction due **palRvlsrd**
 to the Sun's motion with respect to the
 dynamical Local Standard of Rest

Description: This function returns the velocity component in a given direction due to the Sun's motion with respect to the dynamical Local Standard of Rest. The result is +ve when the Sun is receding from the given point on the sky.

Invocation: `double palRvlsrd(double r2000, double d2000)`

Arguments:

r2000 = double (Given)
 J2000.0 mean RA (radians)
d2000 = double (Given)
 J2000.0 mean Dec (radians)

Returned Value:

Component of "peculiar" solar motion in direction R2000,D2000 (km/s).

Notes:

- The Local Standard of Rest used here is the "dynamical" LSR, a point in the vicinity of the Sun which is in a circular orbit around the Galactic centre. The Sun's motion with respect to the dynamical LSR is called the "peculiar" solar motion.
- There is another type of LSR, called a "kinematical" LSR. A kinematical LSR is the mean standard of rest of specified star catalogues or stellar populations, and several slightly different kinematical LSRs are in use. The Sun's motion with respect to an agreed kinematical LSR is known as the "standard" solar motion. To obtain a radial velocity correction with respect to an adopted kinematical LSR use the routine `sla_RVLSRK`.

Reference:

- Delhaye (1965), in "Stars and Stellar Systems", vol 5, p73.

palRvlsrk	Velocity component in a given direction due to the Sun's motion with respect to an adopted kinematic Local Standard of Rest	palRvlsrk
------------------	---	------------------

Description: This function returns the velocity component in a given direction due to the Sun's motion with respect to an adopted kinematic Local Standard of Rest. The result is +ve when the Sun is receding from the given point on the sky.

Invocation: `double palRvlsrk(double r2000, double d2000)`

Arguments:

r2000 = double (Given)
J2000.0 mean RA (radians)

d2000 = double (Given)
J2000.0 mean Dec (radians)

Returned Value:

Component of "standard" solar motion in direction R2000,D2000 (km/s).

Notes:

- The Local Standard of Rest used here is one of several "kinematical" LSRs in common use. A kinematical LSR is the mean standard of rest of specified star catalogues or stellar populations. The Sun's motion with respect to a kinematical LSR is known as the "standard" solar motion.
- There is another sort of LSR, the "dynamical" LSR, which is a point in the vicinity of the Sun which is in a circular orbit around the Galactic centre. The Sun's motion with respect to the dynamical LSR is called the "peculiar" solar motion. To obtain a radial velocity correction with respect to the dynamical LSR use the routine `sla_RVLSRD`.

Reference:

- Delhaye (1965), in "Stars and Stellar Systems", vol 5, p73.

palSubet	Remove the E-terms from a pre IAU 1976 catalogue RA,Dec	palSubet
-----------------	--	-----------------

Description: Remove the E-terms (elliptic component of annual aberration) from a pre IAU 1976 catalogue RA,Dec to give a mean place.

Invocation: `void palSubet (double rc, double dc, double eq, double *rm, double *dm);`

Arguments:

rc = double (Given)
 RA with E-terms included (radians)
dc = double (Given)
 Dec with E-terms included (radians)
eq = double (Given)
 Besselian epoch of mean equator and equinox
rm = double * (Returned)
 RA without E-terms (radians)
dm = double * (Returned)
 Dec without E-terms (radians)

Notes:

Most star positions from pre-1984 optical catalogues (or derived from astrometry using such stars) embody the E-terms. This routine converts such a position to a formal mean place (allowing, for example, comparison with a pulsar timing position).

See Also:

Explanatory Supplement to the Astronomical Ephemeris, section 2D, page 48.

palSupgal	Convert from supergalactic to galactic coordinates	palSupgal
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Description: Transformation from de Vaucouleurs supergalactic coordinates to IAU 1958 galactic coordinates

Invocation: `void palSupgal (double dsl, double dsb, double *dl, double *db);`

Arguments:

dsl = double (Given)
 Supergalactic longitude.
dsb = double (Given)
 Supergalactic latitude.
dl = double * (Returned)
 Galactic longitude.
db = double * (Returned)
 Galactic latitude.

See Also:

- de Vaucouleurs, de Vaucouleurs, & Corwin, Second Reference Catalogue of Bright Galaxies, U. Texas, page 8.
- Systems & Applied Sciences Corp., Documentation for the machine-readable version of the above catalogue, Contract NAS 5-26490.

(These two references give different values for the galactic longitude of the supergalactic origin. Both are wrong; the correct value is L2=137.37.)

palUe2el Universal elements to heliocentric osculating **palUe2el**
elements

Description: Transform universal elements into conventional heliocentric osculating elements.

Invocation: `void palUe2el (const double u[13], int jformr, int *jform, double
 *epoch, double *orbinc, double *anode, double *perih, double *aorq, double *e,
 double *aorl, double *dm, int *jstat);`

Arguments:

u = const double [13] (Given)

Universal orbital elements (Note 1) (0) combined mass (M+m) (1) total energy of the orbit (alpha) (2) reference (osculating) epoch (t0) (3-5) position at reference epoch (r0) (6-8) velocity at reference epoch (v0) (9) heliocentric distance at reference epoch (10) r0.v0 (11) date (t) (12) universal eccentric anomaly (psi) of date, approx

jformr = int (Given)

Requested element set (1-3; Note 3)

jform = int * (Returned)

Element set actually returned (1-3; Note 4)

epoch = double * (Returned)

Epoch of elements (TT MJD)

orbinc = double * (Returned)

inclination (radians)

anode = double * (Returned)

longitude of the ascending node (radians)

perih = double * (Returned)

longitude or argument of perihelion (radians)

aorq = double * (Returned)

mean distance or perihelion distance (AU)

e = double * (Returned)

eccentricity

aorl = double * (Returned)

mean anomaly or longitude (radians, JFORM=1,2 only)

dm = double * (Returned)

daily motion (radians, JFORM=1 only)

jstat = int * (Returned)

status: 0 = OK

- 1 = illegal combined mass
- 2 = illegal JFORMR
- 3 = position/velocity out of range

Notes:

- The "universal" elements are those which define the orbit for the purposes of the method of universal variables (see reference 2). They consist of the combined mass of the two bodies, an epoch, and the position and velocity vectors (arbitrary reference frame) at that epoch. The parameter set used here includes also various quantities that can, in fact, be derived from the other information. This approach is taken to avoiding unnecessary computation and loss of accuracy. The supplementary quantities are (i) alpha, which is proportional to the total energy of the orbit, (ii) the heliocentric distance at epoch, (iii) the outwards component of the velocity at the given epoch, (iv) an estimate of psi, the "universal eccentric anomaly" at a given date and (v) that date.
- The universal elements are with respect to the mean equator and equinox of epoch J2000. The orbital elements produced are with respect to the J2000 ecliptic and mean equinox.
- Three different element-format options are supported:

Option JFORM=1, suitable for the major planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = longitude of perihelion, curly pi (radians) AORQ = mean distance, a (AU) E = eccentricity, e AORL = mean longitude L (radians) DM = daily motion (radians)

Option JFORM=2, suitable for minor planets:

EPOCH = epoch of elements (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = mean distance, a (AU) E = eccentricity, e AORL = mean anomaly M (radians)

Option JFORM=3, suitable for comets:

EPOCH = epoch of perihelion (TT MJD) ORBINC = inclination i (radians) ANODE = longitude of the ascending node, big omega (radians) PERIH = argument of perihelion, little omega (radians) AORQ = perihelion distance, q (AU) E = eccentricity, e

- It may not be possible to generate elements in the form requested through JFORMR. The caller is notified of the form of elements actually returned by means of the JFORM argument:

JFORMR JFORM meaning

1 1 OK - elements are in the requested format 1 2 never happens 1 3 orbit not elliptical
 2 1 never happens 2 2 OK - elements are in the requested format 2 3 orbit not elliptical
 3 1 never happens 3 2 never happens 3 3 OK - elements are in the requested format

- The arguments returned for each value of JFORM (cf Note 6: JFORM may not be the same as JFORMR) are as follows:

JFORM 1 2 3 EPOCH t0 t0 T ORBINC i i i ANODE Omega Omega Omega PERIH curly
pi omega omega AORQ a a q E e e AORL L M - DM n - -

where:

t0 is the epoch of the elements (MJD, TT) T " epoch of perihelion (MJD, TT) i " inclination (radians) Omega " longitude of the ascending node (radians) curly pi " longitude of perihelion (radians) omega " argument of perihelion (radians) a " mean distance (AU) q " perihelion distance (AU) e " eccentricity L " longitude (radians, 0-2pi) M " mean anomaly (radians, 0-2pi) n " daily motion (radians)

- means no value is set
- At very small inclinations, the longitude of the ascending node ANODE becomes indeterminate and under some circumstances may be set arbitrarily to zero. Similarly, if the orbit is close to circular, the true anomaly becomes indeterminate and under some circumstances may be set arbitrarily to zero. In such cases, the other elements are automatically adjusted to compensate, and so the elements remain a valid description of the orbit.

See Also:

- Sterne, Theodore E., "An Introduction to Celestial Mechanics", Interscience Publishers Inc., 1960. Section 6.7, p199.
- Everhart, E. & Pitkin, E.T., Am.J.Phys. 51, 712, 1983.

palUe2pv Heliocentric position and velocity of a planet, **palUe2pv**
asteroid or comet, from universal elements

Description: Heliocentric position and velocity of a planet, asteroid or comet, starting from orbital elements in the "universal variables" form.

Invocation: `void palUe2pv(double date, double u[13], double pv[6], int *jstat);`

Arguments:

date = double (Given)

TT Modified Julian date (JD-2400000.5).

u = double [13] (Given & Returned)

Universal orbital elements (updated, see note 1) given (0) combined mass (M+m) " (1) total energy of the orbit (alpha) " (2) reference (osculating) epoch (t0) " (3-5) position at reference epoch (r0) " (6-8) velocity at reference epoch (v0) " (9) heliocentric distance at reference epoch " (10) r0.v0 returned (11) date (t) " (12) universal eccentric anomaly (psi) of date

jstat = int * (Returned)

status: 0 = OK

- 1 = radius vector zero
- 2 = failed to converge

Notes:

- The "universal" elements are those which define the orbit for the purposes of the method of universal variables (see reference). They consist of the combined mass of the two bodies, an epoch, and the position and velocity vectors (arbitrary reference frame) at that epoch. The parameter set used here includes also various quantities that can, in fact, be derived from the other information. This approach is taken to avoiding unnecessary computation and loss of accuracy. The supplementary quantities are (i) alpha, which is proportional to the total energy of the orbit, (ii) the heliocentric distance at epoch, (iii) the outwards component of the velocity at the given epoch, (iv) an estimate of psi, the "universal eccentric anomaly" at a given date and (v) that date.
- The companion routine is *palEl2ue*. This takes the conventional orbital elements and transforms them into the set of numbers needed by the present routine. A single prediction requires one call to *palEl2ue* followed by one call to the present routine; for convenience, the two calls are packaged as the routine *sla_PLANEL*. Multiple predictions may be made by again calling *palEl2ue* once, but then calling the present routine multiple times, which is faster than multiple calls to *palPlanel*.
- It is not obligatory to use *palEl2ue* to obtain the parameters. However, it should be noted that because *palEl2ue* performs its own validation, no checks on the contents of the array *U* are made by the present routine. in the TT timescale (formerly Ephemeris Time, ET) and is a Modified Julian Date (JD-2400000.5). units (solar masses, AU and canonical days). The position and velocity are not sensitive to the choice of reference frame. The *palEl2ue* routine in fact produces coordinates with respect to the J2000 equator and equinox.
- The algorithm was originally adapted from the EPHSLA program of D.H.P.Jones (private communication, 1996). The method is based on Stumpff's Universal Variables.
- Reference: Everhart, E. & Pitkin, E.T., Am.J.Phys. 51, 712, 1983.